

## **A STUDY OF VISCOELASTIC SURFACE USING INDEPENDENT AND DEPENDENT SHEAR RATE**

**Dr. Surya Narain Prasad**

**M.Sc. (Mathematics), Ph.D., SSSUTMS, Sehore**

**Madhya Pradesh, India**

### **Abstract**

The impact of surface viscoelasticity effects on the compelling properties of materials, for example, viable twisting solidness of plates or shells. Viscoelastic properties in the region of the surface can vary from the properties of the mass material. This distinction impacts the conduct of Nano structural elements. Specifically, the surface viscoelastic stresses are liable for the size-dependent dissemination of Nano sized structures. The enthusiasm for the examination of surface effects is as of late developed corresponding to the Nano mechanics. The surface effects assume a significant job for such Nano sized materials as films, Nano permeable materials.

**Keywords:** viscoelasticity, surface, shear rate, polymer

### **Introduction**

Viscoelastic fluids (for instance, polymeric melts and solutions) have stream properties that are to a limited extent gooey and to some extent flexible. The nearness of versatile stresses can produce dangers, even in idleness less stream, that don't emerge in Newtonian fluids. These are frequently depicted as 'absolutely flexible' hazards. Visco-Elastic materials display both thick and versatile properties; in a simply Hookean flexible strong the stress relating to a given strain is free of time, though for viscoelastic substances the stress will steadily disperse. As opposed to absolutely gooey fluids, then again, viscoelastic liquids stream when exposed to stress however some portion of their misshapening is step by step endless supply of the stress. Instances of viscoelastic liquids incorporate bitumen's Lethersich, Flour Dough Schofield and ScottBlair, Napalm and comparable jams, polymers and polymer melts, for example, nylon, and numerous polymer arrangements. Toms and Strawbridge, discovered viscoelastic conduct in arrangements containing somewhere in the range of 1 and 10% of profoundly polymerized methyl methacrylate in toluene, pyridine, cyclohexanone and n-butyl acetic acid derivation. Oldroyd,

has indicated that scatterings of one Newtonian liquid in another may prompt emulsions having both thick and versatile attributes.

Shear-rate subordinate surface viscosities (one sort of non-Newtonian consistent shear conduct) have been dealt with utilizing summed up Newtonian constitutive conditions, where the stress might be a nonlinear capacity of strain rate however not of the deformational history. The Powell-Eyring model has, for instance, been utilized. Both the summed up Newtonian and basic rate-sort of constitutive conditions are restricted in pertinence, the previous to consistent shear and the last to little deformational flows. The model introduced here applies to both of these flows just as to non-consistent, enormous deformational flows. The model would thus be able to be utilized to relate diverse surface rheological trials including an interface having a blurring memory (a viscoelastic interface).

Surface dynamic particles specially adsorb at an interface, regularly shaping a thick, stuffed monolayer despite the fact that the focuses in the adjoining mass stages are very little. The nearness of little amounts of surfactants may not quantifiably change the mass rheological properties, yet mechanical properties might be modified significantly in the interfacial area. For instance, it is feasible for the surface consistency to show shear-rate reliance despite the fact that the mass stages might be Newtonian. Likewise, viscoelastic conduct in which the surface will in general snap endless supply of stress has been watched. It is the motivation behind this paper to bring together such marvels.

### **Mathematical Model**

The mathematical explanation of protection of energy in a two-stage framework gives a limit condition wherein the rheological conduct of the interface is presented, The condition which administers the movement of each mass stage and with which the limit condition is related is [1].

$$p \frac{Dv}{Dt} = -\nabla P - \nabla \cdot \tau + pg$$

$$N(P^I - P^{II}) + N \cdot (\tau^I - \tau^{II}) = -2H\sigma N - \nabla \cdot \sigma$$

Since the constitutive condition created here applies to fluid interfaces, and since just fluid mass stages are thought of, vital conditions for mechanical harmony are that

$$\tau = 0$$

$$\tau^I = 0$$

Specifically, if these conditions are applied to above Equation, the typical part of that condition decreases to the LaPlace condition which characterizes the weight bounce over an interface.

### **The Surface Constitutive Equation**

The model introduced here is fundamentally a changed, two dimensional form of a constitutive condition created by Tanner and Simmons for incompressible, viscoelastic, mass stages. In any case, the current model isn't restricted to incompressible interfaces.

$$\tau^s = \int_0^\infty \left\{ M(s, \Psi) L(s) + \frac{K(s, \Psi) - M(s, \Psi)}{2} \text{tr} L(s) 1_s \right\} d_s \quad (1)$$

where

$$M(s, \Psi), K(s, \Psi) = \begin{cases} m(s) k(s) & \text{if } \Psi \leq B^2 \\ 0 & \text{if } \Psi > B^2 \end{cases} \quad (2)$$

$k(s)$ ,  $m(s)$  = memory capacities which rot with  $s$ . In basic terms, the model depicts an interface whose memory blurs with time but at the same time is constrained to distortions of a specific size, to be specific, those for which  $\Psi \leq B^2$ .

Equation (1) is a complex equation, and the predicted flow obtain by bringing it into the limit condition isn't promptly discernable. Notwithstanding, it ought to be noticed this is the main general constitutive equation that has been proposed for an interface. Its actual helpfulness must be surveyed by contrasting predicted and watched conduct.

### **Steady share surface flow**

Let us consider a level interface lying in the x-y plane of a Cartesian facilitate framework x, y, z. assume that the movement in the interface is with the end goal that

$$v_x = v_x(y) \quad (3)$$

$$v_x = 0 \quad (4)$$

$$\tau^s xy = -\eta(\gamma) \frac{dv_x}{dy} \quad (5)$$

$$\eta(\gamma) = \int_0^{B/\gamma} sm(s) ds \quad (6)$$

$\eta$  depends on the surface shear rate

$\gamma(\gamma = \left| \frac{dv_x}{dy} \right|)$  that is, the film is non-Newtonian.

A careful investigation of steady shear flow uncovers the predicted presence of surface typical stresses. No notice of this chance has been proposed in the writing, despite the fact that in a portion of our investigations utilizing the profound channel surface viscometer we have watched conduct which might just be ascribed to the presence of surface typical stresses. The model predicts that for the steady shear flow above

$$-r^s_{xx} = r^s_{yy} = \theta(\gamma) \left( \frac{dv_x}{dy} \right) \quad (7)$$

where the normal stress coefficient  $\theta$  is given by

$$\theta(\gamma) = 1/2 \int_0^{B/\gamma} s^2 m(s) ds \quad (8)$$

No investigation has yet been accounted for quantitatively building up the presence of surface ordinary stresses; nonetheless, utilizing Equation (8) related to a six-boundary model proposed in an ensuing segment, the extent of the impact can be assessed expecting, obviously, that the model is illustrative of the genuine framework.

### **Small Deformational Surface Flows**

For any small deformational surface flow the model reduces to

$$\tau^s = \int_0^\infty \left\{ m(s)G(s) + \frac{k(s)-m(s)}{2} trG(s)I_s \right\} ds \quad (9)$$

For instance of a little deformational surface, think about a plane, sinusoidal shear of little sufficiency. Once more, assume the interface lies in the x-y plane of a Cartesian organize framework x, y, z. However, this time guess that

$$v_x = \text{Im}\{v(y)e^{i\omega t}\} \quad (10)$$

$$v_y = 0 \quad (11)$$

where  $v(y)$  = a difficult task of  $y$ ,  $i = \sqrt{-1}$ , and  $\text{Im}\{ \}$  = invented component. For this type of surface flow, the model predicts that

$$r^s xy = -\text{Im}\left\{\eta^o(\omega) \frac{dv}{dy} e^{i\omega t}\right\} \quad (12)$$

$$r^s xx = r^s yy = 0 \text{ (approximately)} \quad (13)$$

$$\eta^o(\omega) = \text{complex surface viscosity} \quad (14)$$

$$= \eta' - i\left(\frac{G'}{\omega}\right) \quad (15)$$

$$\eta'(\omega) = \text{dynamic surface viscosity}$$

$$= \int_0^\infty \frac{m(s) \sin(\omega s)}{\omega} ds \quad (16)$$

Note that the material capacities  $\eta(\gamma), \theta(\gamma)$  and  $G'$  are completely related through the shear memory work  $m(s)$ . This memory capacity can, on a basic level, be assessed by estimating the complex thickness as an element of recurrence and playing out a backwards Fourier change. In any case, a simpler methodology is to characterize  $m(s)$  by a rough useful structure and to assess those parameters which are reliant on the idea of the interfacial film utilizing exploratory information.

Figure 1 illustrates the shear rate and recurrence reliance of  $\eta(\gamma)$  and  $\eta(\omega)$  predicted by the six-boundary model for four theoretical films. Moderately, film A has a little surface consistency and long memory film B a little surface thickness and short memory, film C a huge surface thickness and short memory, and film D a huge surface thickness and long memory.

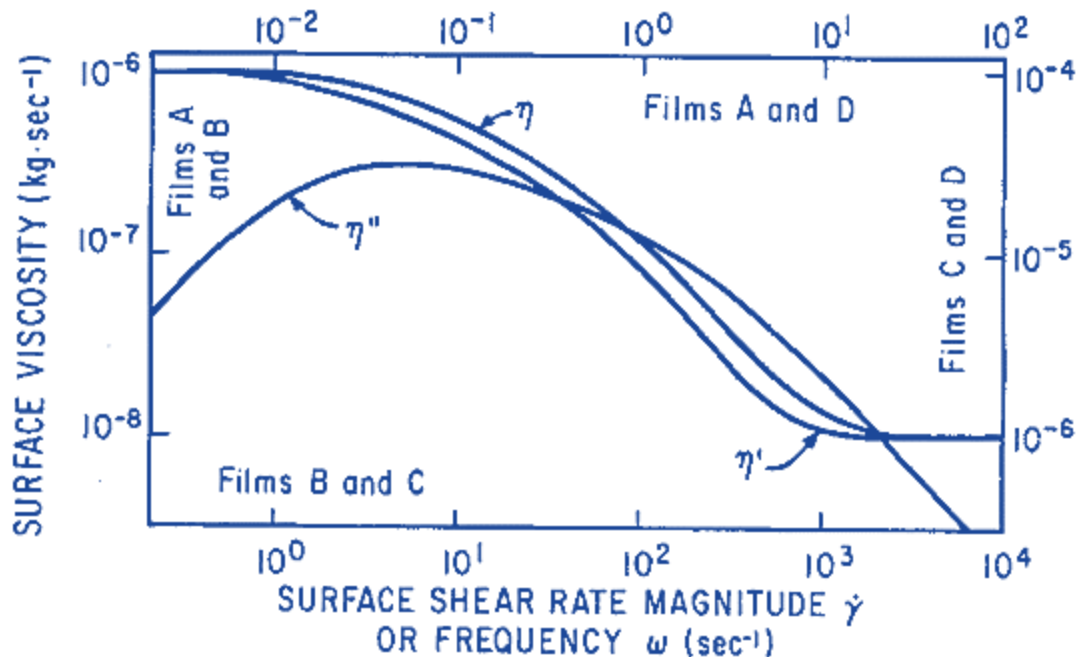


Figure 1. Four six-parameter films

Gardner and Schechter have proposed a strategy for assessing the six parameters  $\alpha$ ,  $\beta$ ,  $\lambda$ . B utilizing information acquired from the profound channel surface rheometer (Burton and Mannheimer, and Schechter) changed with the goal that the floor can be made to waver at different frequencies just as pivot consistently as was initially proposed.

### Conclusion

The constitutive equation introduced in this paper is the first proposed which has the capacity of speaking to complex viscoelastic surfaces. The model predicts various intriguing marvels, some of which presently can't seem to be tentatively affirmed. For instance, surface typical stresses, not considered previously, are predicted. Moreover, the dynamic surface pressure of a viscoelastic interface is portrayed. Investigations of an adsorbed poly vinyl film have been led in a profound channel surface rheometer and the watched conduct saw as all around connected by the six-boundary model.

## **References**

Akoussan, K., Boudaoud, H., Daya, E. M., Koutsawa, Y. & Carrera, E. Sensitivity analysis of the damping properties of viscoelastic composite structures according to the layers thicknesses. *Compos. Struct.* 149, 11–25 (2016).

Bilasse, M., Azrar, L. & Daya, E. M. Complex modes based numerical analysis of viscoelastic sandwich plates vibrations. *Comput. Struct.* 89, 539–555 (2011).

Chazeau, L., Brown, J. D., Yanyo, L. C. & Sternstein, S. S. Modulus recovery kinetics and other insights into the Payne effect for filled elastomers. *Polym. Compos.* 21, 202–222 (2000).

Choi, H. & Kim, J. New installation scheme for viscoelastic dampers using cables. *Can. J. Civ. Eng.* 37, 1201–1211 (2010).

De Fenza, A., Monaco, E., Amoroso, F. & Lecce, L. Experimental approach in studying temperature effects on composite material structures realized with viscoelastic damping treatments. *J. Vib. Control* 22, 358–370 (2016).

Eftekhari, M. & Fatemi, A. On the strengthening effect of increasing cycling frequency on fatigue behavior of some polymers and their composites: Experiments and modeling. *Int. J. Fatigue* 87, 153–166 (2016).

Kelly, T. E. *In-structure damping and energy dissipation*. (Holmes Consulting Group, 2001).

Kim, J., Ryu, J. & Chung, L. Seismic performance of structures connected by viscoelastic dampers. *Eng. Struct.* 28, 183–195 (2006).

Lion, A., Kardelky, C. & Haupt, P. On the frequency and amplitude dependence of the Payne effect: Theory and experiments. *Rubber Chem. Technol.* 76, 533–547 (2003).

Min, K.-W., Kim, J. & Lee, S.-H. Vibration tests of 5-storey steel frame with viscoelastic dampers. *Eng. Struct.* 26, 831–839 (2004).

Oncu-Davas, S. & Alhan, C. Reliability of semi-active seismic isolation under near-fault earthquakes. *Mech. Syst. Signal Process.* 114, 146–164 (2019).

Rao, M. D. Recent applications of viscoelastic damping for noise control in automobiles and commercial airplanes. *J. Sound Vib.* 262, 457–474 (2003).

Suhr, J., Koratkar, N., Keblinski, P. & Ajayan, P. Viscoelasticity in carbon nanotube composites. *Nat. Mater.* 4, 134–137 (2005).

Suhr, J., Koratkar, N., Keblinski, P. & Ajayan, P. Viscoelasticity in carbon nanotube composites. *Nat. Mater.* 4, 134–137 (2005).

Vergassola, G., Boote, D. & Tonelli, A. On the damping loss factor of viscoelastic materials for naval applications. *Ships Offshore Struct.* 13, 466–475 (2018).

Zhou, X. Q., Yu, D. Y., Shao, X. Y., Zhang, S. Q. & Wang, S. Research and applications of viscoelastic vibration damping materials: A review. *Compos. Struct.* 136, 460–480 (2016).